

So now, we wrote down the momentum of the system of our rocket at time, t , and the movement of the system of the rocket at time t plus Δt .

Let's make some simplifications in our notation just to make our calculations a little more easy to read.

So the first thing we want to do is we want to say that the mass of the rocket at time, t -- this is the mass of the rocket plus the mass of the fuel in the rocket at time, t .

We're just going to denote that by m_r .

And keep in mind that, when you write the mass at time t plus Δt , we'll write that as the mass at time t plus Δt m_r . This is precisely how you define a differential.

Even if this quantity is negative, you always write the difference.

$m_r(t + \Delta t) - m_r(t) = \Delta m_r$. That's how we write a differential Δm_r of the rocket.

So the mass of the rocket at time, t , looks simpler-- $m_r + \Delta m_r$.

So those are two ways of simplifying our expressions for the terms that are appearing here and there.

Now, the next thing was, recall from our mass conservation, that we had the condition that Δm_{fuel} was equal to minus Δm_{rocket} .

So now, we'll take those two simplifications, and now we'll write down our system momentum at time, t .

That's very simple.

$m_r v_r$ at time t , and we'll now write the momentum at time t plus Δt .

Well, we have the first piece, which is $m_r + \Delta m_r$ times the velocity of the rocket at time t plus Δt .

Now, be careful here because we're going to use our conservation of mass condition to replace Δm_{fuel} with minus Δm_{rocket} , and we'll use our expression for the velocity of fuel in the ground frame of the rocket.

So we have minus Δm_{rocket} times the velocity u plus $v_r(t + \Delta t)$.

And this simplification, we'll write equations 1 and equation 2, will enable us to apply the momentum principle in a very transparent way.

And that's what we'll do next.